

Section 6: Sequences and proof**Exercise**

- n is a positive integer. Prove that $n^3 - n^2$ is always even.
- Prove that the product of three consecutive integers is always be a multiple of 6.
- Prove that the square of any odd number is always 1 more than a multiple of 8.
- Write down the first four terms of each sequence defined below, starting with $n = 1$ in each case.
 - $3n - 1$
 - $n^2 - 1$
 - $3n^2 - 2n + 1$
- Find a formula for the n th term of each the linear sequences below.
 - 2, 5, 8, 11, ...
 - 10, 8, 6, 4, ...
- Find a formula for the n th term of each the quadratic sequences below.
 - 3, 9, 17, 27, 39, ...
 - 2, 4, 14, 28, 46, ...
 - 7, 12, 15, 16, 15, ...
- For each of the following sequences, find the 1st term, the 5th term, the 100th term, and the limit of the sequence as $n \rightarrow \infty$.
 - n th term $= \frac{2n+5}{4n-1}$
 - n th term $= \frac{1-6n}{2n+3}$
- The n th term of a sequence is given by the formula $n^2 + 2n - 5$.
Prove that 1000 cannot be a term of the sequence.
- A sequence has all its terms positive.
As $n \rightarrow \infty$, the n th term of the sequence approaches 3.
 - Give a possible formula for the n th term of an increasing sequence with the properties above.
 - Give a possible formula for the n th term of a decreasing sequence with the properties above.